

# Signals of CP Violation Beyond the MSSM in Higgs Physics

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Based on arXiv:1107.3814 with Wolfgang Altmannshofer, Marcela Carena  
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# Outline

- The Higgs sector in the MSSM and the Little Hierarchy Problem
  - Beyond the MSSM
- Additional sources of CP violation
  - CP violation beyond the MSSM
- Higgs Collider Phenomenology
- Closing Remarks

# The MSSM

$$W_{MSSM} = \mu \hat{H}_u \cdot \hat{H}_d + y_u^{ij} \hat{u}_i^c \hat{H}_u \cdot \hat{Q}_{Lj} - y_d^{ij} \hat{d}_i^c \hat{H}_d \cdot \hat{Q}_{Lj} - y_\tau^{ij} \hat{e}_i^c \hat{H}_d \cdot \hat{E}_{Lj}$$

## What can it do:

- It is a solution to the “Hierarchy Problem”
- Light Higgs mimics SM Higgs in production and decay
- Bound on Higgs mass at tree-level proportional to gauge couplings

$$M_{h^0} \leq M_Z \cos 2\beta$$

In the Higgs decoupling limit, the bound on the MSSM Higgs is the same as that of the SM Higgs from LEP  $\rightarrow$  114 GeV

Need for large radiative corrections originating from SUSY particles... heavy stops above 1 TeV

Creates a fine tuning in the mass parameters since  $m_{\tilde{t}}$  provides the cutoff for the quadratically divergent Higgs mass parameter

➡ Introduces a “Little Hierarchy problem”

## Beyond the MSSM

- Effective Field theory with SUSY preserving and SUSY breaking dimension 5 operators

Dine, Seiberg and Thomas;  
See also:

Carena, Kong, Ponton, and  
Zurita;

Antoniadis, Dudas, Ghilencea,  
and Tziveloglou;

$$W \supset \mu \hat{H}_u \hat{H}_d + \frac{\omega}{2M} (\hat{H}_u \hat{H}_d)^2$$

**NLO contributions arise from Kahler potential terms  $O(1/M^2)$  small for consistent effective field theory yet relevant**

# Beyond the MSSM

- Incorporate gauge singlets  
i.e. **SMSSM** (Delgado, Kolda, Olson, AP 2010):

$$W_{\hat{S}} = (\lambda \hat{S} + \mu) \hat{H}_u \hat{H}_d + \frac{\mu_s}{2} \hat{S}^2$$

$$m_{h^0}^2 \simeq m_Z^2 \cos^2 2\beta + \frac{2\lambda^2 v^2}{\mu_s} (2\mu \sin 2\beta - A_\lambda \sin^2 2\beta)$$

# Hunting for additional sources of CP violation



# Motivations for additional sources of CP violation

Standard Model has two sources of CP violation

## 1. CKM matrix: Constrained by unitarity

– probed through the K and B meson systems

## 2. Arising from strong dynamics: $L \supset \frac{\alpha_s}{8\pi} \Theta G \tilde{G}$ Constrained by neutron electric dipole moment (EDM)

Problem in reproducing CP violation from the baryon asymmetry in the universe (BAU)

$$\frac{n_B}{n_\gamma} = (1.5 - 6.3) \times 10^{-10}$$



## CP violation in the MSSM Higgs sector

- Radiatively induced
- Phases may occur in  $\mu, A_f, m_{1/2}$
- Mixing among CP-even and CP-odd Higgs

MSSM can be used as a model for electroweak baryogenesis to generate the BAU... However

- EWBG requires a light right handed stop... (strong 1st order phase transition)
- MSSM requires a large stop  
➡ Fine tuning



Beyond the MSSM with CP violation

# CP violating BMSSM

Effective field theory approach:

- Leading higher dimensional operators added to MSSM Higgs sector

$$W = W_{Yukawa} + \mu \hat{H}_u \hat{H}_d + \frac{w}{2M} (\hat{H}_u \hat{H}_d)^2$$

- SUSY breaking term in the Lagrangian

$$L \supset \alpha \frac{\omega m_s}{2M} (H_u H_d)^2$$

# CP violating BMSSM

Effective field theory approach:

- Leading higher dimensional operators added to MSSM Higgs sector

$$W = W_{Yukawa} + \mu \hat{H}_u \hat{H}_d + \frac{\omega}{2M} (\hat{H}_u \hat{H}_d)^2$$

- SUSY breaking term in the Lagrangian

$$L \supset \alpha \frac{\omega m_s}{2M} (H_u H_d)^2$$

$\omega$  and  $\alpha$  are complex order one parameters;  
and  $m_s$  is the scale of the SUSY breaking  
terms of the BMSSM physics

At the renormalizable level, the tree level potential is given by:

$$\begin{aligned}
 V_{\text{ren}} &= V_{\text{MSSM}} + \left( \alpha \frac{\omega m_S}{2M} (H_u H_d)^2 - \frac{\omega \mu^*}{M} (H_u H_d) (H_u^\dagger H_u + H_d^\dagger H_d) + h.c. \right) \\
 &= (m_{H_u}^2 + |\mu|^2) H_u^\dagger H_u + (m_{H_d}^2 + |\mu|^2) H_d^\dagger H_d + (B\mu (H_u H_d) + h.c.) \\
 &+ \frac{g_2^2}{8c_W} (H_d^\dagger H_d)^2 + \frac{g_2^2}{8c_W} (H_u^\dagger H_u)^2 - \frac{g_2^2}{4c_W} (H_d^\dagger H_d) (H_u^\dagger H_u) + \frac{g_2^2}{2} (H_u^\dagger H_d) (H_d^\dagger H_u) \\
 &+ \left( \alpha \frac{\omega m_S}{2M} (H_u H_d)^2 - \frac{\omega \mu^*}{M} (H_u H_d) (H_u^\dagger H_u + H_d^\dagger H_d) + h.c. \right)
 \end{aligned}$$

- Parametrize the complex coefficients as

$$\lambda_5 = |\lambda_5| e^{i\phi_5} \equiv \frac{\alpha \omega m_s}{M}$$

$$\lambda_6 = |\lambda_6| e^{i\phi_6} \equiv \frac{\omega \mu^*}{M}$$

1/M operator in the Superpotential leads to additional non-renormalizable operators

$$V_6 = \frac{\lambda_8}{M^2} (H_u H_d) (H_u^\dagger H_d^\dagger) (H_u^\dagger H_u) + \frac{\lambda'_8}{M^2} (H_u H_d) (H_u^\dagger H_d^\dagger) (H_d^\dagger H_d)$$

where  $\lambda_8 = |\omega|^2$

- Crucial in bounding potential from below
- At the  $1/M^2$ , Kahler terms can be incorporated → lead to larger Higgs masses

Carena, Kong, Ponton and Zurita

## Electroweak Symmetry Breaking:

- The Higgs fields are parametrized as follow:

$$H_u^T = e^{i\theta_u} \left( H_u^+, \frac{v_u + h_u + ia_u}{\sqrt{2}} \right) \quad H_d^T = e^{i\theta_d} \left( \frac{v_d + h_d + ia_d}{\sqrt{2}}, H_d^- \right)$$

$$v_u = v \sin \beta$$

$$v_d = v \cos \beta$$

- Relative phase can be rotated away by a U(1) transformation and  $\theta = \theta_u + \theta_d$  is physical

$$\frac{\partial V}{\partial \text{Re}H_u} = \frac{\partial V}{\partial \text{Re}H_d} = \frac{\partial V}{\partial \theta} = 0$$

- where the third condition leads to:

$$v^2 c_\beta s_\beta |\lambda_5| \sin(\phi_5 + 2\theta) + v^2 |\lambda_6| \sin(\phi_6 + \theta) - 2B\mu \sin \theta = 0$$

- Minimization conditions do not necessarily lead to a unique solution
- Second minima along D-flat direction
- Metastability



## Spectrum at tree-level

In the absence of CP violation we have:

$$\begin{pmatrix} h \\ H \end{pmatrix} = \begin{pmatrix} c_\alpha & -s_\alpha \\ s_\alpha & c_\alpha \end{pmatrix} \begin{pmatrix} h_u \\ h_d \end{pmatrix}, \quad \begin{pmatrix} G \\ A \end{pmatrix} = \begin{pmatrix} s_\beta & -c_\beta \\ c_\beta & s_\beta \end{pmatrix} \begin{pmatrix} a_u \\ a_d \end{pmatrix}$$

- CP violation leads to scalar-pseudoscalar mixing:

$$M_H^2 = \begin{pmatrix} M_h^2 & 0 & M_{hA}^2 \\ 0 & M_H^2 & M_{HA}^2 \\ M_{hA}^2 & M_{HA}^2 & M_A^2 \end{pmatrix}$$

$$M_{hA}^2 = -\frac{v^2}{2} (c_{\beta+\alpha} |\lambda_5| \sin(\phi_5 + 2\theta) - 2s_{\beta-\alpha} |\lambda_6| \sin(\phi_6 + \theta))$$

$$M_{HA}^2 = -\frac{v^2}{2} (s_{\beta+\alpha} |\lambda_5| \sin(\phi_5 + 2\theta) - 2c_{\beta-\alpha} |\lambda_6| \sin(\phi_6 + \theta))$$

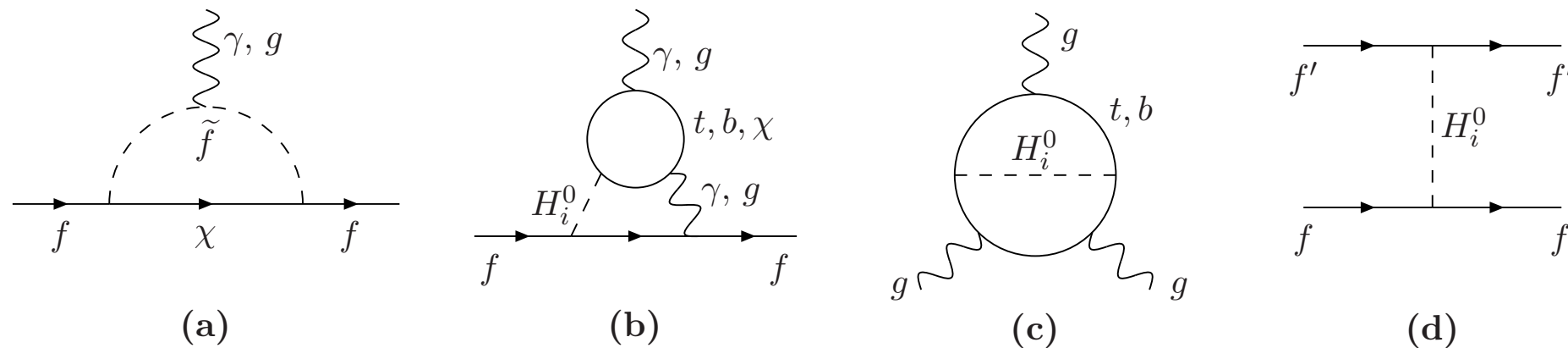
## Spectrum at tree-level

$$M_H^2 = \begin{pmatrix} M_h^2 & 0 & M_{hA}^2 \\ 0 & M_H^2 & M_{HA}^2 \\ M_{hA}^2 & M_{HA}^2 & M_A^2 \end{pmatrix}$$

- The mass matrix is diagonalized by an orthogonal matrix  $O_{ij}$  such that

$$O^T M_H^2 O = \text{diag}(M_{H_1}^2, M_{H_2}^2, M_{H_3}^2)$$

# Constraints arising from EDM's



- Highly sensitive probes of CP violation
- Lead to tight constraints on new sources of CP violation

at 95% C.L:

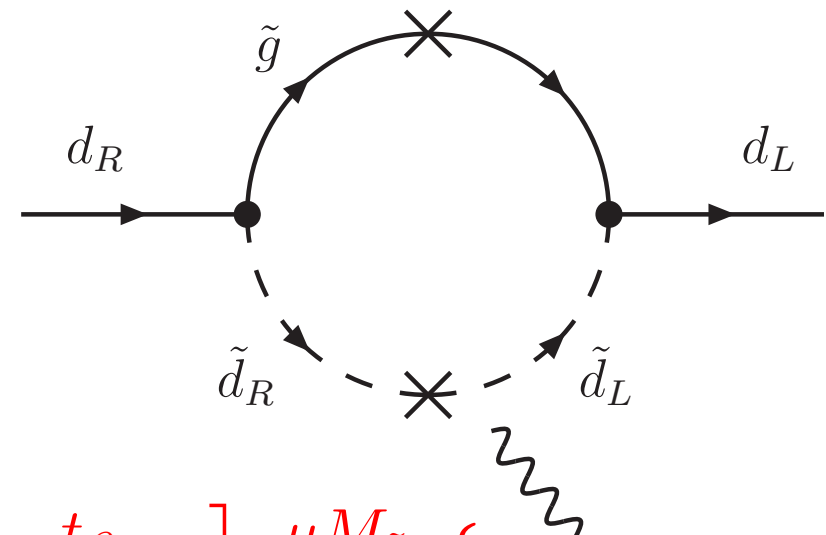
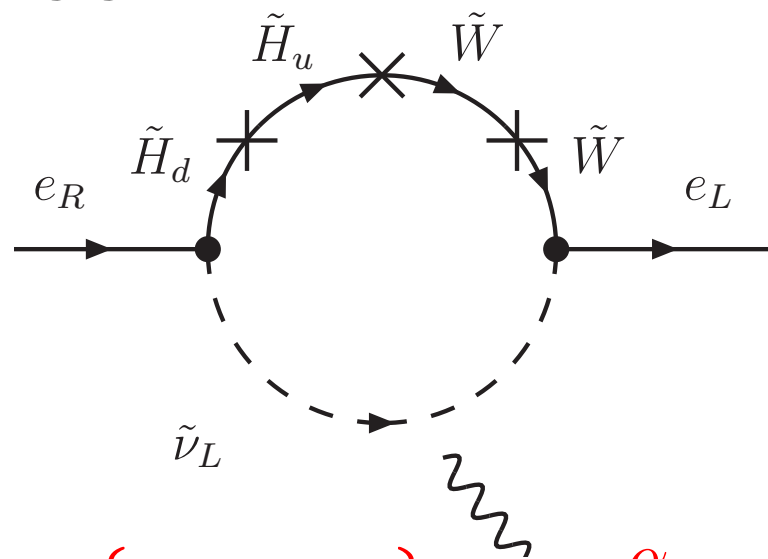
$$|d_n| < 3.5 \times 10^{-26} ecm$$

$$|d_{Tl}| < 1.1 \times 10^{-24} ecm$$

$$|d_{Hg}| < 2.9 \times 10^{-29} ecm$$

# Constraints arising from EDM's

- One loop EDMs mainly induced by phase of the Higgs vev



$\left\{ d_d^{\tilde{g}}/e, \tilde{d}_d^{\tilde{g}} \right\} \simeq \frac{\alpha_s}{4\pi} m_d \text{Im} \left[ \textcircled{e^{i\theta}} \frac{t_\beta}{1 + \epsilon_d t_\beta} \right] \frac{\mu M_{\tilde{g}}}{\tilde{m}^4} \left\{ f_d(x_g), \tilde{f}_d(x_g) \right\}$

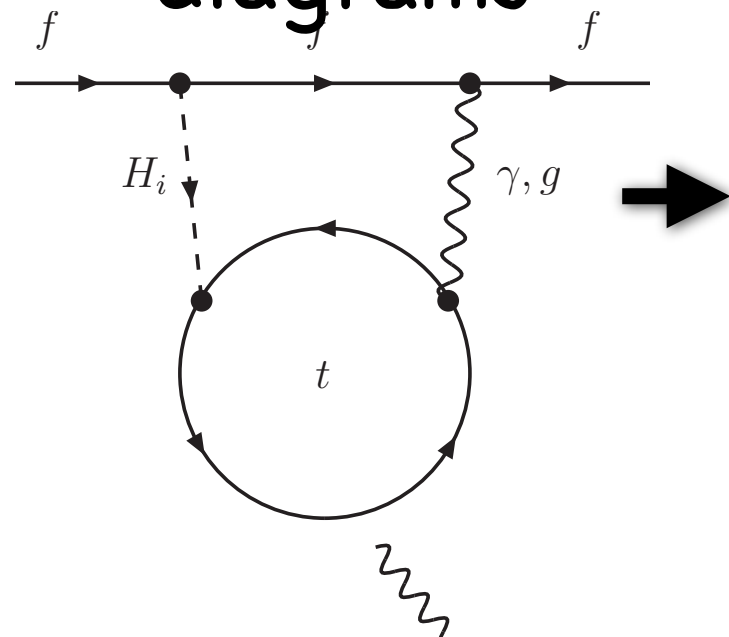
$\Rightarrow$

$d_e^{\tilde{H}}/e \simeq \frac{\alpha_2}{4\pi} m_e \text{Im} \left[ \textcircled{e^{i\theta}} \frac{t_\beta}{1 + \epsilon_\ell t_\beta} \right] \frac{\mu M_2}{\tilde{m}^4} f_e(x_\mu, x_2)$

- $\epsilon$  terms due to  $\tan \beta$  resummation from non-holomorphic corrections to down quark and electron Yukawa couplings
- One loop contributions are  $\tan \beta$  enhanced

# Constraints arising from EDM's

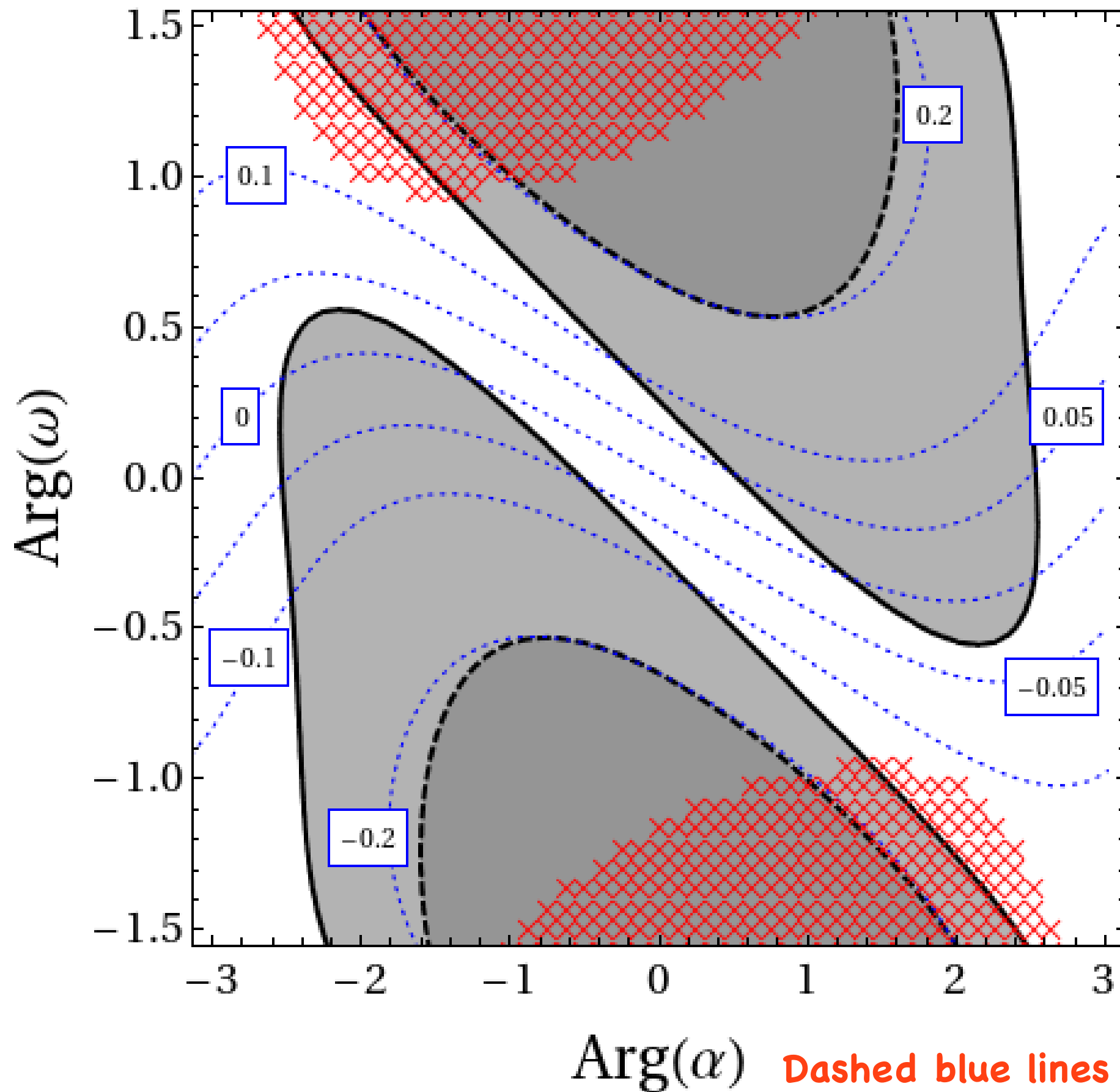
- Two-loop contributions are due to Bar-Zee diagrams



$$d_e^{(2)t}/e = \frac{\alpha_2 \alpha_{em}}{16\pi^2} \frac{4}{3} m_e \operatorname{Re} \left[ \frac{\tan \beta}{1 + \epsilon_\ell t_\beta} \right] \frac{m_t^2}{M_W^2} \\ \times \sum_{i=1}^3 \frac{1}{M_{H_i}^2} O_{3i} \left( \frac{s_\alpha}{s_\beta} O_{2i} + \frac{c_\alpha}{s_\beta} O_{1i} \right) f \left( \frac{m_t^2}{M_{H_i}^2} \right)$$

- Sensitive to mixing between scalar and pseudoscalar Higgs through  $O_{ij}$
- Two-loop contributions can be as large as 1-loop contributions for relatively light Higgs masses

$$|\alpha| = 1$$



$$\tan \beta = 2$$

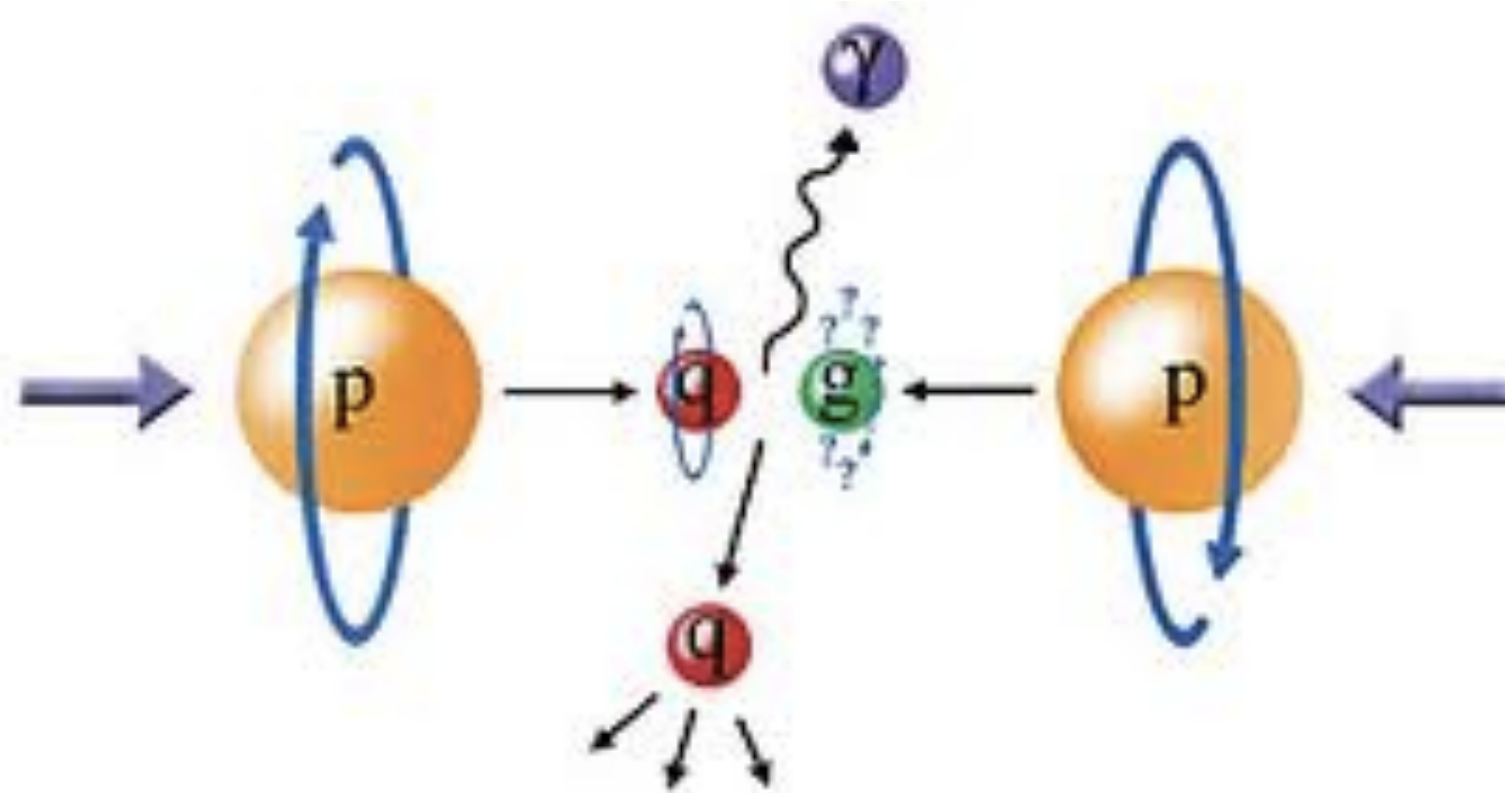
$$\omega = 1$$

$$\mu = m_s = 150 \text{ } 150$$

$$M_{H^+} = 200 \text{ GeV}$$

$$M = 1.5 \text{ TeV}$$

Dashed blue lines correspond to different values of the phase of the Higgs vev



# Higgs Collider Phenomenology

# LEP and Tevatron Bounds

- Worked with effective couplings normalized to SM

$$\xi_{\gamma\gamma H_i}^2 = \frac{\Gamma(H_i \rightarrow \gamma\gamma)_{LO}}{\Gamma(H_i \rightarrow \gamma\gamma)_{LO}^{SM}}$$

$$\xi_{gg H_i}^2 = \frac{\Gamma(H_i \rightarrow gg)_{LO}}{\Gamma(H_i \rightarrow gg)_{LO}^{SM}} \approx \frac{\sigma(gg \rightarrow H_i)}{\sigma(gg \rightarrow H_i)^{SM}}$$

5-20%

- Compatibility with LEP and Tevatron searches is checked using Higgsbounds

Bechtle, Brein, Heinemeyer, Werglein, Williams

- Incorporating also latest Tevatron exclusion T. Aaltonen et al. 2011

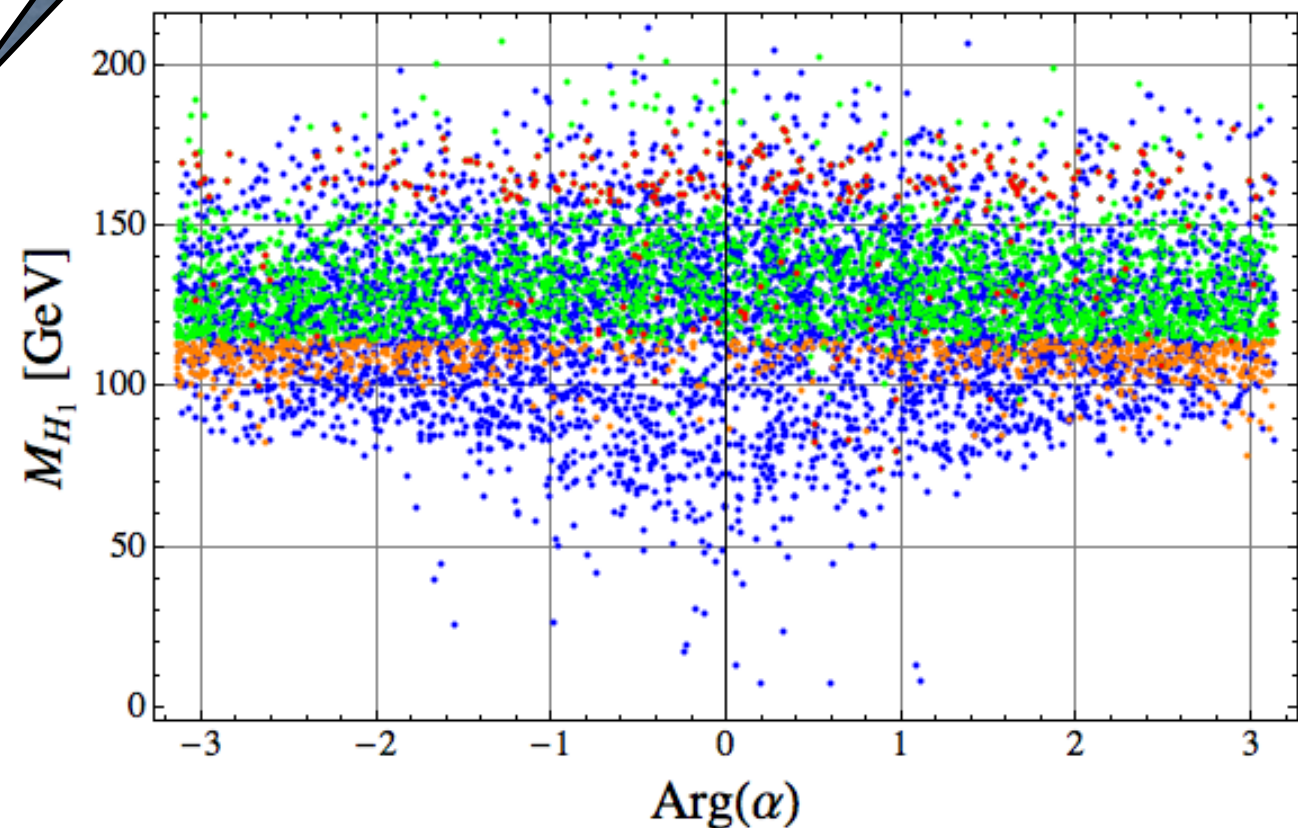
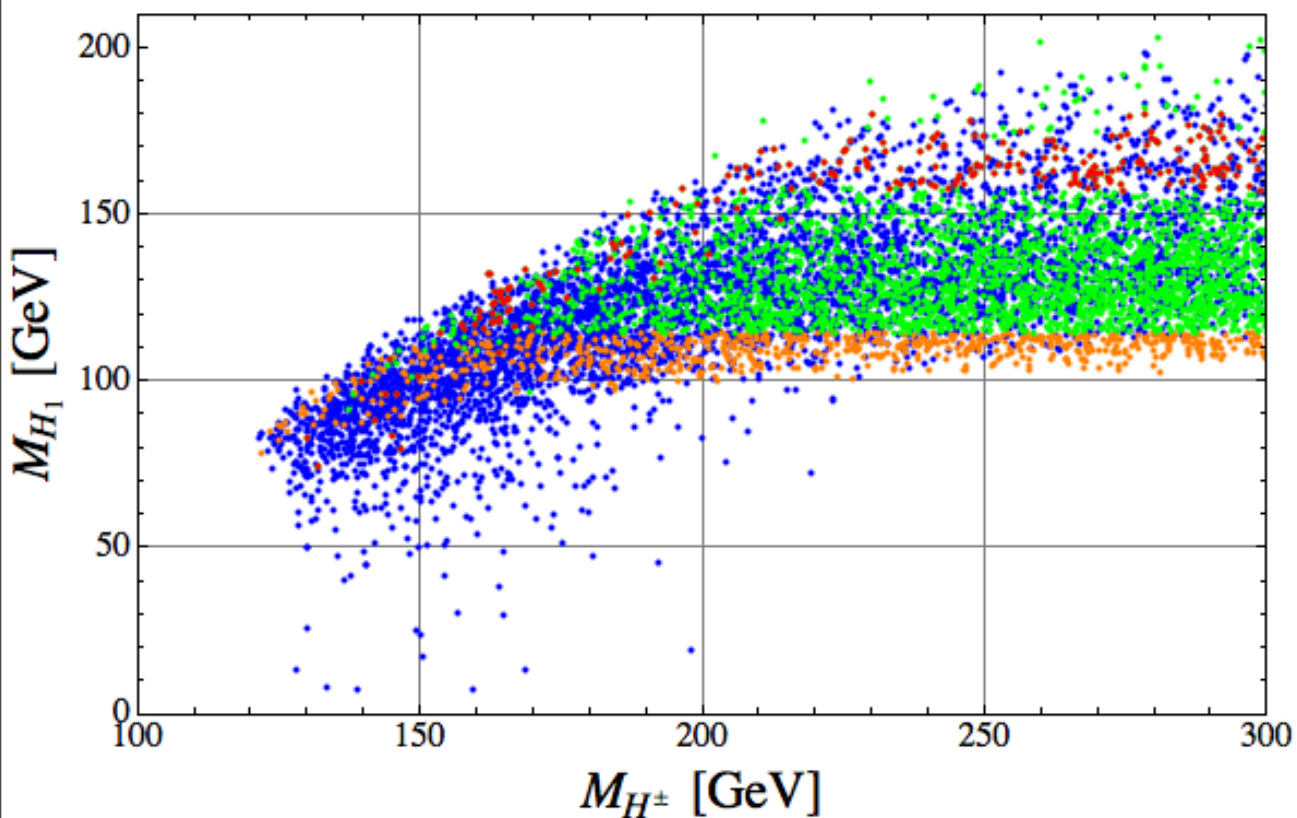


## Parameter Scan:

- Excluded by EDMs
- Excluded by LEP
- Excluded by Tevatron
- Allowed

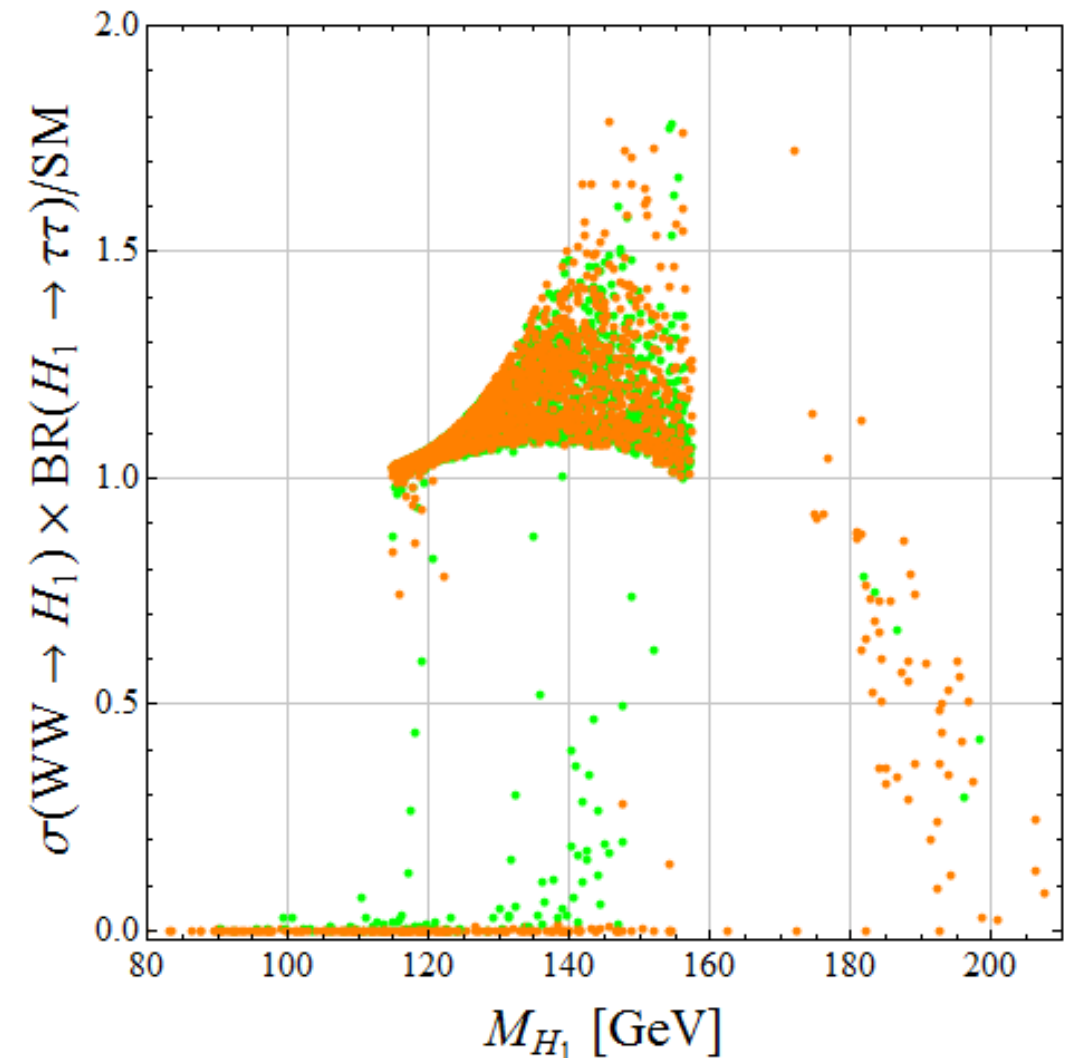
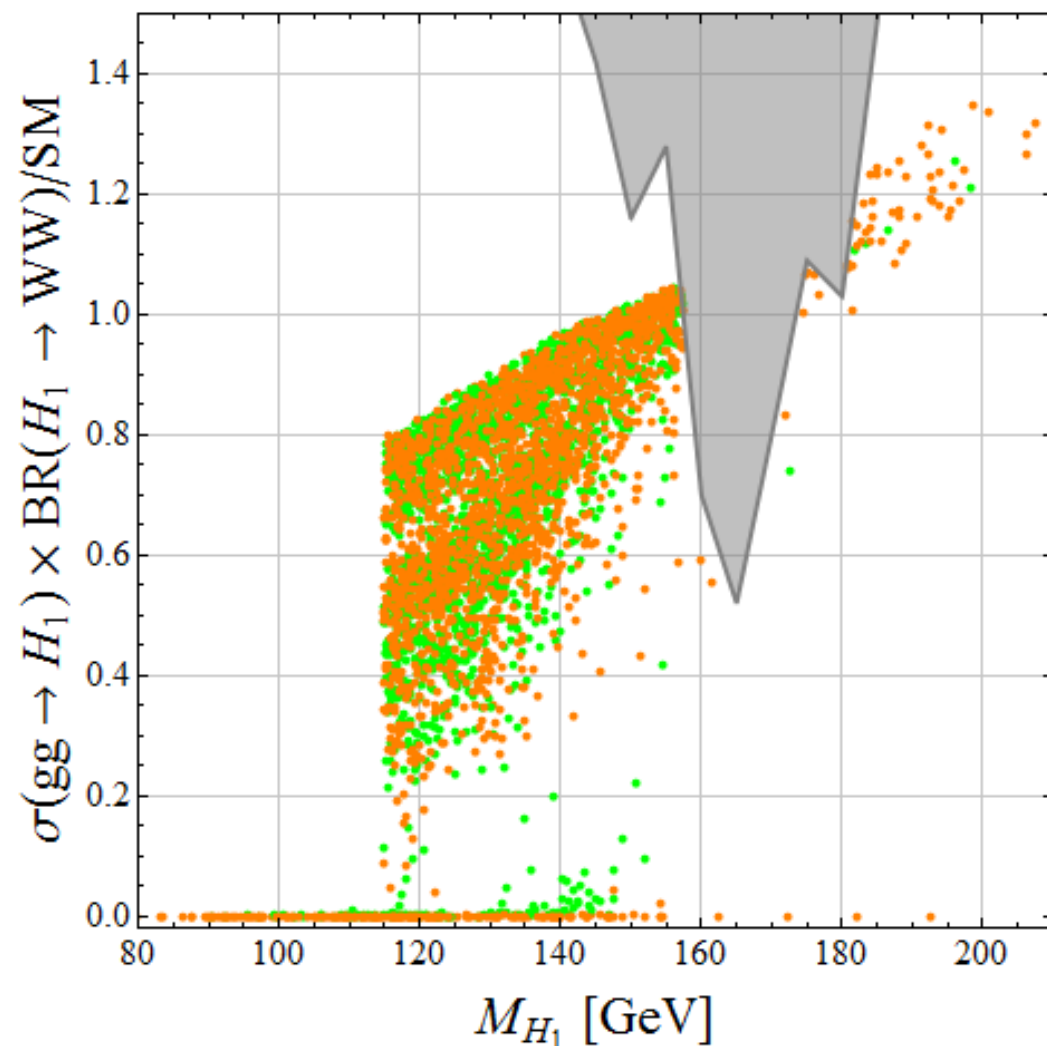
$$\begin{aligned} \text{Arg}(\alpha) &\in [0, 2\pi] \\ \omega &= (0.5 \rightarrow 2.) e^{-\frac{i}{5} \text{Arg}(\alpha)} \\ M &\in [1, 3] \text{ TeV} \\ M_{H^\pm} &\leq 350 \text{ GeV} \end{aligned}$$

$$\tan \beta = 2, m_s = \mu = 150 \text{ GeV}, m_{\tilde{q}} = 800 \text{ GeV}$$



# Generic features of the Parameter Scan

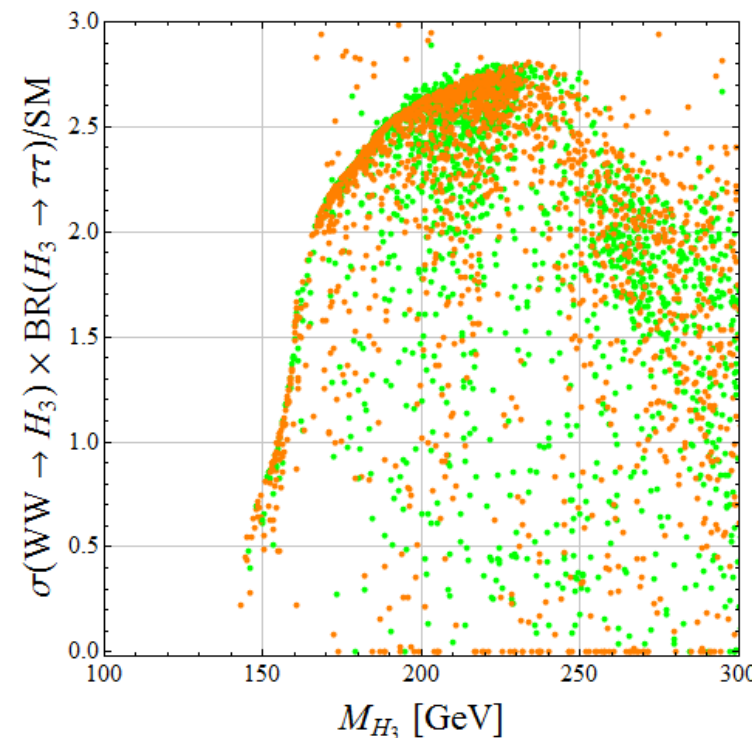
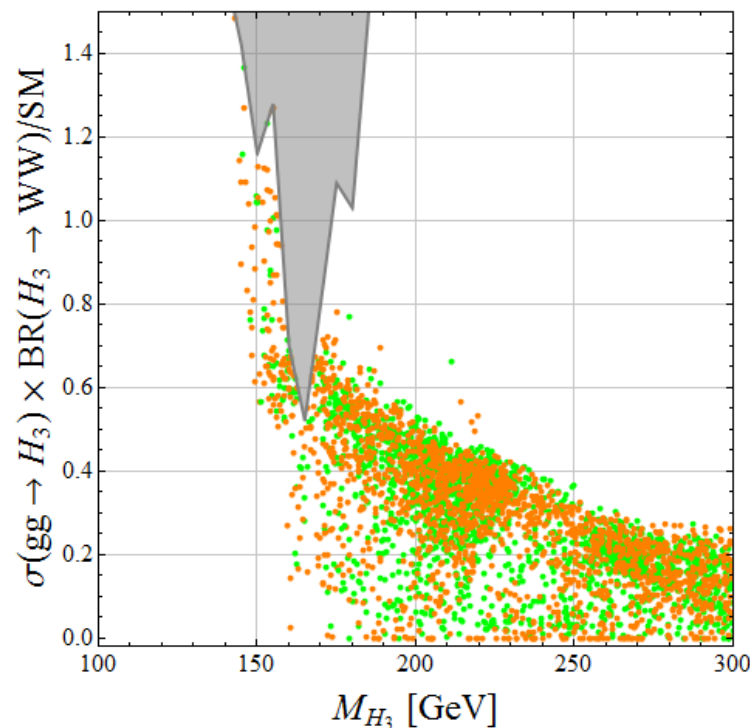
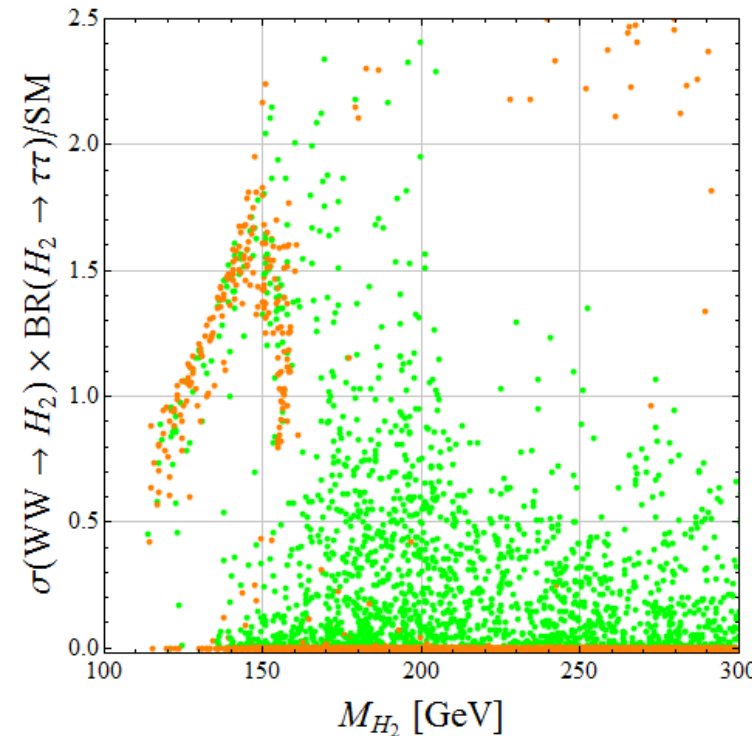
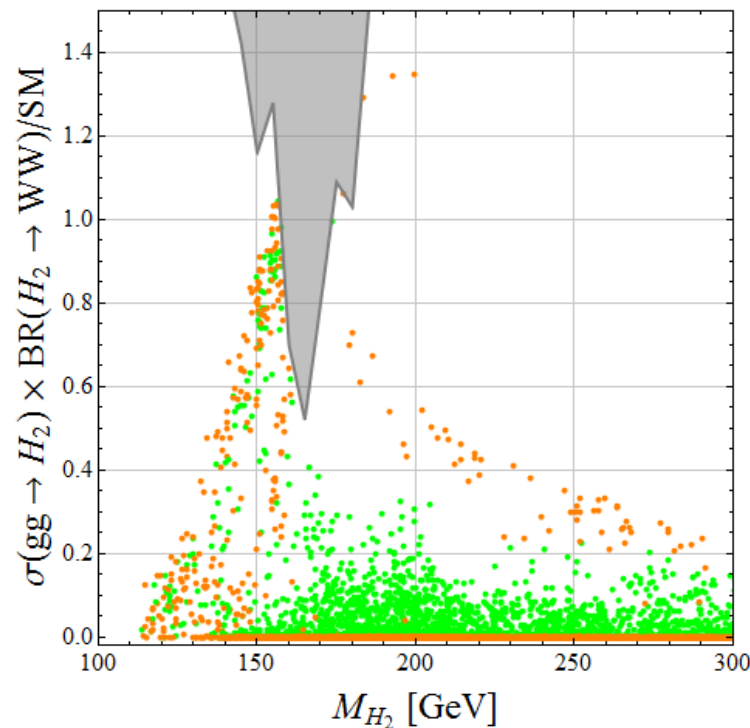
● CP conserving ● CP violating



- WW channel promising in both scenarios
- For masses below 140 GeV,  $\sigma(gg \rightarrow H_1) \cdot BR(H_1 \rightarrow WW)$  suppressed compared to SM, but may be possible to probe at Tevatron and LHC
- The  $\tau\tau$  channel is slightly enhanced for wide range of masses... LHC not yet sensitive

# Generic features of the Parameter Scan

● CP conserving ● CP violating



● Heavier Higgs boson can be discovered in the WW channel

● Absence of a pure pseudoscalar... mixing even leads to sizable enhancement in the WW production cross section

●  $\tau\tau$  channel enhanced with respect to SM for masses above 150 GeV where  $\sigma(WW \rightarrow H_{2,3}) \cdot BR(H_{2,3} \rightarrow \tau\tau)$  are too small to allow for detection



# CP violating scenarios: Benchmark points

## Scenario A:

| Scenario III  | $H_1$     | $H_2$       | $H_3$      |
|---|-----------|-------------|------------|
| $M_{H_i}$ [GeV]                                       | 145       | 169         | 198        |
| $\xi_{ZZH_i}^2$                                       | 0.94      | 0.02        | 0.04       |
| $\xi_{ggH_i}^2$                                       | 0.68      | 0.59        | 0.53       |
| $\text{BR}(H_i \rightarrow bb)$                       | 42% (23%) | 59% (0.8%)  | 15% (0.2%) |
| $\text{BR}(H_i \rightarrow WW)$                       | 45% (60%) | 31% (97%)   | 62% (74%)  |
| $\text{BR}(H_i \rightarrow ZZ)$                       | 6% (8%)   | 0.7% (2.4%) | 20% (26%)  |
| $\text{BR}(H_i \rightarrow \gamma\gamma) \times 10^4$ | 15 (17)   | 0.8 (1.6)   | 0.2 (0.5)  |

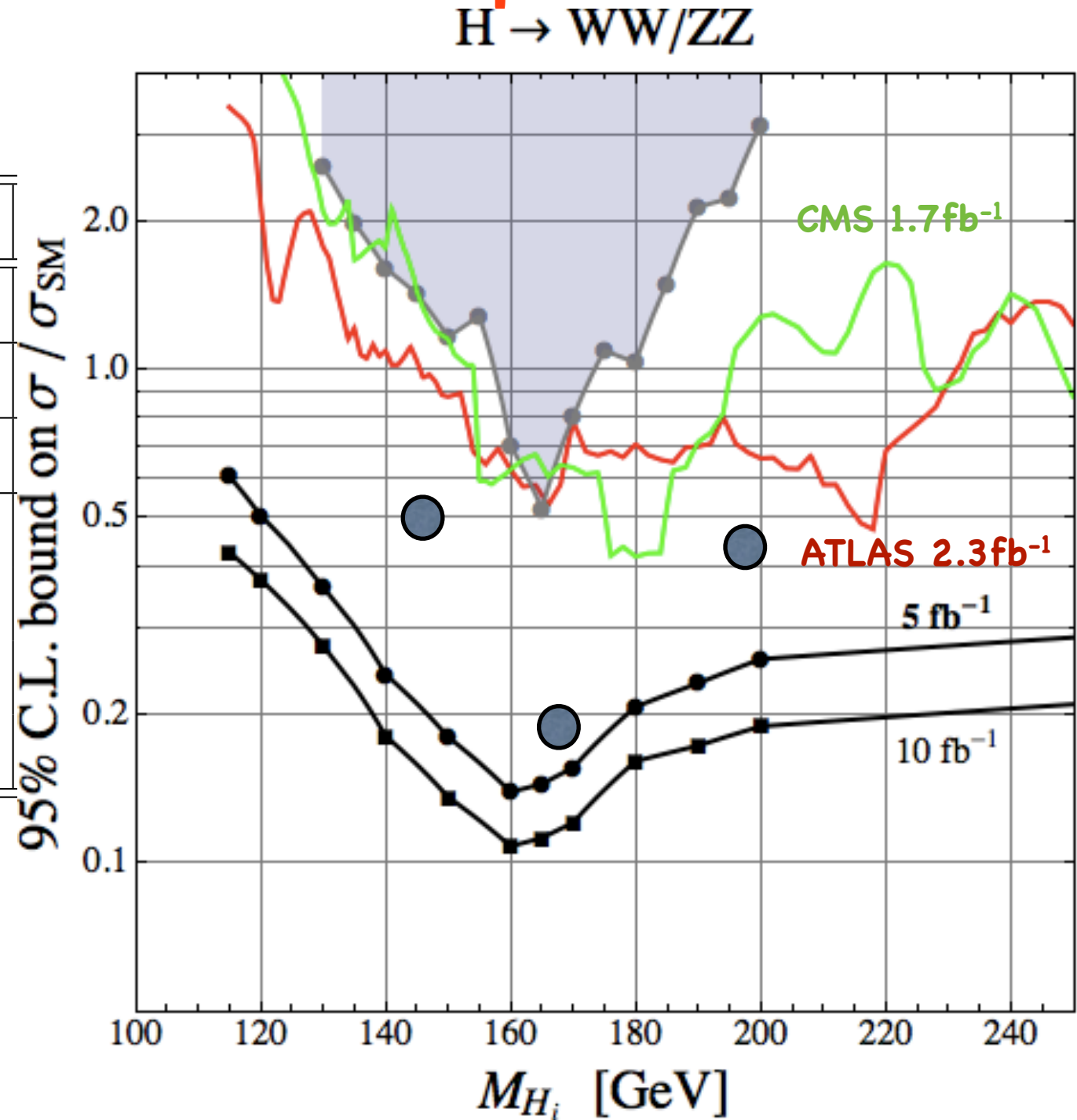
|                      | Sc. III   |
|----------------------|-----------|
| $ \alpha $           | 1         |
| $ \omega $           | 1.5       |
| $\text{Arg}(\alpha)$ | $\pi/3$   |
| $\text{Arg}(\omega)$ | $-\pi/15$ |
| $\tan \beta$         | 2         |
| $M_{H^\pm}$ [GeV]    | 190       |
| $M$ [TeV]            | 2.5       |
| $\mu$ [GeV]          | 150       |
| $m_S$ [GeV]          | 150       |

- All three neutral Higgs bosons have masses above 145 GeV with significant branching ratios into WW
- This scenario cannot be achieved in the MSSM

# CP violating scenarios: Benchmark points

## Scenario A:

|   |           |
|---|-----------|
| Scenario III  | $H_1$     |
| $M_{H_i}$ [GeV]                                       | 145       |
| $\xi_{ZZH_i}^2$                                       | 0.94      |
| $\xi_{ggH_i}^2$                                       | 0.68      |
| $\text{BR}(H_i \rightarrow bb)$                       | 42% (23%) |
| $\text{BR}(H_i \rightarrow WW)$                       | 45% (60%) |
| $\text{BR}(H_i \rightarrow ZZ)$                       | 6% (8%)   |
| $\text{BR}(H_i \rightarrow \gamma\gamma) \times 10^4$ | 15 (17)   |



- Scenario testable with  $5\text{fb}^{-1}$  of data at the LHC

# CP violating scenarios: Benchmark points

## Scenario B:

| Scenario II   | $H_1$     | $H_2$     | $H_3$     |
|---|-----------|-----------|-----------|
| $M_{H_i}$ [GeV]                                       | 147       | 150       | 162       |
| $\xi_{ZZH_i}^2$                                       | 0.62      | 0.32      | 0.06      |
| $\xi_{ggH_i}^2$                                       | 0.41      | 0.53      | 0.39      |
| $\text{BR}(H_i \rightarrow bb)$                       | 69% (22%) | 72% (16%) | 65% (2%)  |
| $\text{BR}(H_i \rightarrow WW)$                       | 20% (63%) | 17% (69%) | 26% (94%) |
| $\text{BR}(H_i \rightarrow ZZ)$                       | 3% (8%)   | 2% (8%)   | 1% (3%)   |
| $\text{BR}(H_i \rightarrow \gamma\gamma) \times 10^4$ | 6 (16)    | 3 (13)    | 0.5 (4)   |

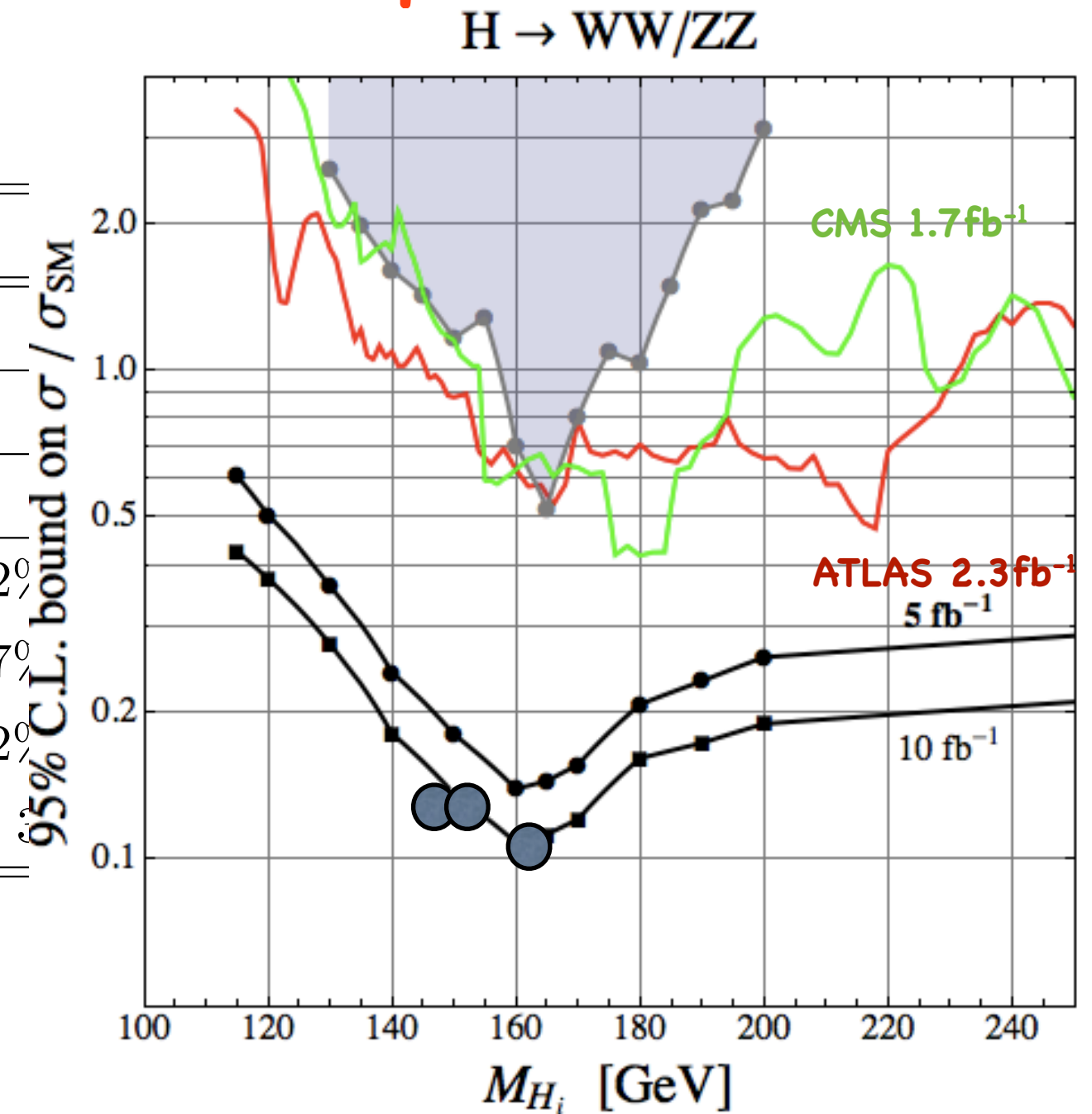
|                      | Sc. II    |
|----------------------|-----------|
| $ \alpha $           | 0.8       |
| $ \omega $           | 1.6       |
| $\text{Arg}(\alpha)$ | $-2\pi/3$ |
| $\text{Arg}(\omega)$ | $\pi/20$  |
| $\tan \beta$         | 3         |
| $M_{H^\pm}$ [GeV]    | 166       |
| $M$ [TeV]            | 2         |
| $\mu$ [GeV]          | 140       |
| $m_S$ [GeV]          | 100       |

- All three neutral Higgs bosons have masses between 145 and 160 GeV decaying dominantly to  $b\bar{b}$
- Strongly suppressed cross sections in the channel  $gg \rightarrow H_i \rightarrow \gamma\gamma$
- Associated production with Higgs decays to  $\tau\tau$  larger than SM but difficult to probe given the large Higgs masses

# CP violating scenarios: Benchmark points

## Scenario B:

| Scenario II   | $H_1$     |     |
|---|-----------|-----|
| $M_{H_i}$ [GeV]                                       | 147       |     |
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| $\xi_{ggH_i}^2$                                       | 0.41      |     |
| $\text{BR}(H_i \rightarrow bb)$                       | 69% (22%) | 72% |
| $\text{BR}(H_i \rightarrow WW)$                       | 20% (63%) | 17% |
| $\text{BR}(H_i \rightarrow ZZ)$                       | 3% (8%)   | 2%  |
| $\text{BR}(H_i \rightarrow \gamma\gamma) \times 10^4$ | 6 (16)    |     |



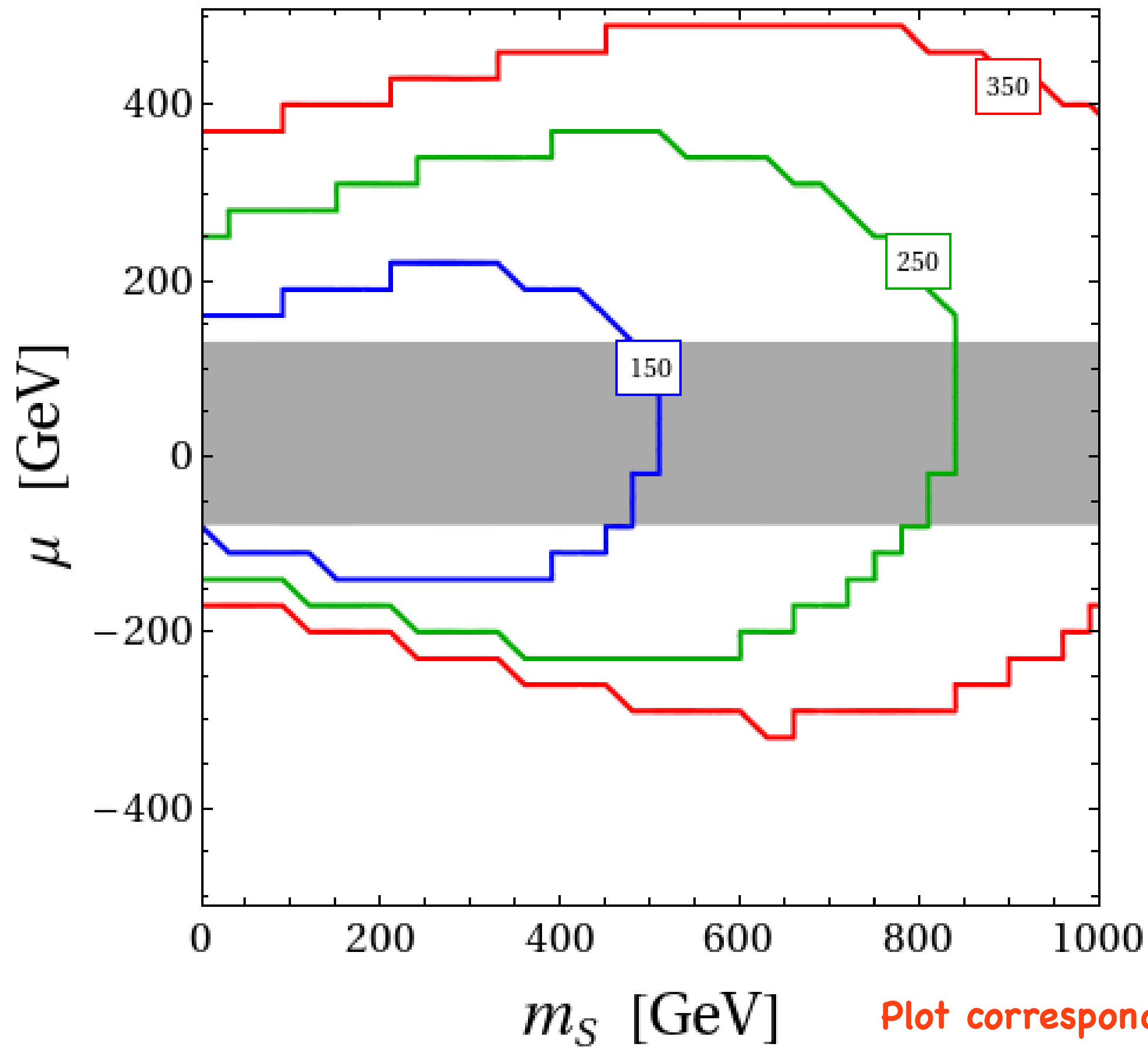
- Might be probed with 5 fb<sup>-1</sup> of data given lack of mass resolution... All three Higgs bosons appear as one

## Closing Remarks

- Introduced two new dimension 5 operators to the MSSM and study their implications as a possible source of CP violation
  - Low  $\tan \beta$  favorable with EDM constraints
  - Sizable couplings of Higgs bosons with weak gauge bosons
- BMSSM with CP violation leads to interesting signals in Higgs collider physics that will be probed very soon
  - Three Higgs bosons with significant branching ratios into  $WW$
  - Three heavy Higgs bosons decaying primarily into  $b\bar{b}$



# Back-up Slides



$$M = 2 \text{ TeV}$$

$$\tan \beta = 2$$

$$|\alpha| = |\omega| = 1$$

Plot corresponding to values for  
the charged Higgs mass of 150,  
250 and 350 GeV